University of South Carolina

Midterm Examination 1 February 10, 2022

Math 142-001/002

Closed book examination	Time: 75 minutes
Name	-

Instructions:

Notes, books, computer, phones, calculators or other aids are **not** allowed. Please write on only one side of each page. If you need more space than is provided, then ask for extra paper from the proctor. Simplify your final answers. Full credit will not be awarded for insufficient accompanying work.

There are 16 + 9 + 9 + 10 + 10 + 6 = 60 points available, but the exam is **out of** 55. (In other words, there are 5 bonus points available)

1. (16 points) Find the following integrals.

(a)
$$\int 3x^3 + 4x^2 - 2x + 7 \ dx$$

(b)
$$\int \frac{1}{x} + e^x + 2^x + \sqrt{x} \, dx$$

(c)
$$\int \sin(\theta) + \cos(\theta) + \tan(\theta) + \sec(\theta) d\theta$$

(d)
$$\int \sec^2(t) + \sec(t)\tan(t) + \frac{1}{1+t^2} + \frac{1}{\sqrt{1-t^2}} dt$$

2. (9 points) Find the following integrals.

(a)
$$\int 3x^2 \cos(x^3) \ dx$$

(b)
$$\int 4\theta \cos(3\theta) \ d\theta$$

(c)
$$\int \tan^2(\theta) \sec^2(\theta) d\theta$$

3. (9 points) Find the following integrals.

(a)
$$\int \frac{\ln(\ln(x))}{x} dx$$

(b)
$$\int x^2 e^x \ dx$$

(c)
$$\int \frac{1}{e^x + e^{-x}} dx$$

4. (10 points) Find $\int \frac{\sqrt{9x^2 - 4}}{x} dx$ for |x| > 2/3.

5. (10 points) Find the following integrals.

(a)
$$\int \frac{1}{x^2 - 3x + 2} dx$$

 $(b) \int \frac{x}{x^2 + 6x + 10} dx$

6. (6 points) Find the integral $\int_{-\infty}^{\infty} \frac{5}{9x^2 + 16} dx$.